

B.Sc. Honours 4th Semester Examination, 2023

PHSACOR08T-PHYSICS (CC8)

Time Allotted: 2 Hours

Full Marks: 40

The figures in the margin indicate full marks.

Candidates should answer in their own words and adhere to the word limit as practicable.

All symbols are of usual significance.

Question No. 1 is compulsory and answer any two from the rest

1. Answer any *ten* questions from the following:

 $2 \times 10 = 20$

- (a) Solve $z^2(1-z^2)=16$, where z is a complex number.
- (b) Find the cube roots of (-1+i).
- (c) Expand $f(z) = \ln(1+z)$ in a Taylor Series about z = 0.
- (d) Find the three dimensional Fourier transform of three dimensional Dirac-delta function.
- (e) For a cylindrically symmetric potential ϕ , find the solution of one dimensional Laplace's equation.
- (f) Show that the product of two symmetric matrices is symmetric if they commute.
- (g) Evaluate e^A where matrix A is given by $A = \begin{bmatrix} 1 & 0 \\ 0 & 2 \end{bmatrix}$.
- (h) For a 2×2 square matrix A, find its eigenvalues in terms of t and d, given Tr(A) = t and det(A) = d.
- (i) If f(s) is Fourier transform of F(t), then show that Fourier transform of

$$F(at)$$
 is $\frac{1}{a}f\left(\frac{s}{a}\right)$.

- (j) If ϕ be a function of r only, then show $\nabla^2 \phi = \frac{d^2 \phi}{dr^2} + \frac{2}{r} \frac{d\phi}{dr}$.
- (k) Show that eigenvalues of an anti Hermitian matrix is either zero or purely imaginary.
- (1) Find the Fourier sine transform of e^{-x} .
- (m) Find the Fourier transform of a Dirac Delta Function $f(x) = \delta(x-a)$, 'a' being some constant.
- (n) Prove that a real matrix is unitary if it is orthogonal.

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- 2. (a) Expand $f(z) = \frac{1}{(z+1)(z+3)}$ in a Laurent series valid for 1 < |z| < 3.
 - (b) Show that the Fourier transform of a Gaussian function is also a Gaussian function.
 - (c) An uncharged conducting sphere of radius R is placed in a uniform electrostatic

 field $\vec{E} = E_0 \hat{k}$. Find the potential outside the sphere using solution of Laplace's equation in spherical polar coordinates.
- 3. (a) Find the characteristic equation of the matrix. 1+2+2

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & 1 \end{bmatrix}$$

and verify Cayley-Hamilton theorem for it. Hence find A^{-1} .

(b) Find the Fourier transform of the function 2

$$f(x) = \begin{cases} 1 & , & \text{for } |x| < a \\ 0 & , & \text{for } |x| > a \end{cases}$$

- (c) Show that $\oint_C \frac{e^{zt}}{z^2 + 1} dz = 2\pi i \sin t$, if t > 0 and C is the circle |z| = 3.
- 4. (a) Two matrices A and B satisfy $(AB)^T + B^{-1}A = 0$. Prove that if B is orthogonal, then A is anti-Symmetric.
 - (b) If a matrix B commutes with a diagonal matrix A, no. two elements of which are equal, show that, B is a diagonal matrix.
 - (c) For the following function locate and name the singularities in the finite z-plane and determine whether they are isolated singularities or not.

$$f(z) = \frac{z}{\left(z^2 + 4\right)^2}$$

- 5. (a) If F(w) be the Fourier transform of a function f(x), then show that the Fourier transform of the derivative of f(x) is -jw F(w).
 - (b) If $w = f(z) = \frac{1+z}{1-z}$, find (i) $\frac{dw}{dz}$ and (ii) determine where f(z) is non analytic.
 - (c) Solve one dimensional heat equation 5

$$\frac{\partial U(x,t)}{\partial t} = h^2 \frac{\partial^2 U(x,t)}{\partial x^2}$$

Using Fourier transform. Given the initial condition u(x, 0) = f(x).

___x__



B.Sc. Honours 4th Semester Examination, 2023

PHSACOR09T-PHYSICS (CC9)

Time Allotted: 2 Hours

Full Marks: 40

The figures in the margin indicate full marks.

Candidates should answer in their own words and adhere to the word limit as practicable.

All symbols are of usual significance.

Question No. 1 is compulsory and answer any two from the rest

1. Answer any *ten* questions from the following:

 $2 \times 10 = 20$

- (a) A pion at rest decays into a muon and a neutrino. Show that the kinetic energy of muon is $T_{\mu} = (m\pi m\mu)^2 c^2 / 2m\pi$.
- (b) What are "space-like interval" and "time-like interval"?
- (c) Show that the Compton wavelength corresponds to the self-energy of an electron.
- (d) Calculate the number of light quanta present in green light of 100 W per m² per second. Given $\lambda = 6000$ Å.
- (e) Show that "the particle and the associated wave packet move together, i.e., move with the same velocity".
- (f) How does a nucleus resembles a liquid drop? Give two points.
- (g) What do you mean by "Boltzmann weight factor"? Write down the relationship between Boltzmann distribution function and this weight factor.
- (h) Calculate the ratio of stimulated to spontaneous emission rates for the wavelength $\lambda = 5900 \text{ Å}$ at 250°C.
- (i) A hydrogen atom is 5.3×10^{-11} m in radius. Use the uncertainty principle to estimate the minimum energy an electron can have in this atom.
- (j) Explain the 'ultraviolet catastrophe' in context of black body radiation.
- (k) The half-life of radon is 3.82 days. What fraction of freshly prepared sample of radon will disintegrate in 10 days?
- (1) Calculate the number of photons emitted per sec. by a 100 watt sodium lamp. $(\lambda = 5893 \text{ Å for sodium}).$
- (m) Calculate the energy of γ -rays emitted in the β -decay of $_{13}Al^{28}$. Given: the end point energy = 2.81 MeV; $M\binom{28}{13}Al$ = 27.9819 u; $M\binom{28}{14}Si^{28}$ = 27.9769 u.
- (n) A nucleus with A = 235 splits into two nuclei of mass numbers in the ratio 2:1. Find the radii of the new nucleus.

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2. (a) What is 'proper time' and 'proper length'?

2

(b) In a frame S, the following two events occur:

3

Event 1:
$$x_1 = x_0$$
, $t_1 = \frac{x_0}{c}$, $y_1 = z_1 = 0$

Event 2:
$$x_2 = 2x_0$$
, $t_2 = \frac{x_0}{2c}$, $y_2 = z_2 = 0$

Find the relative velocity of S' frame relative to S in which the events occur at the same time and what is the t-value?

(c) The position and momentum of 1 keV electron are simultaneously measured. If its position is located to within 1A, find the percentage of uncertainty in its momentum.

3

(d) Establish Bohr's quantization condition on the basis of de Broglie's concept of matter waves.

2

3. (a) What is 'population inversion'? How the population inversion is achieved in the He-Ne gas laser?

1+3

(b) If R be the radius of the nucleus and $\langle r^2 \rangle$ be the mean squared radius of nuclear charge distribution, show that $R^2 = \frac{5}{3} \langle r^2 \rangle$.

2

(c) Calculate the α -disintegration energy for the α -particle with energy 5.76 MeV emitted from the nucleus $_{83}\mathrm{Bi}^{212}$.

2

(d) Prove mass of photon is zero.

2

4. (a) Draw a graph indicating stability line. On this graph indicate the β -active nuclei. 1+1+2 Explain the role of neutrino hypothesis in understanding the β -ray spectrum.

(b) Discuss the features of B.E./A vs. A curve.

3

3

(c) What are the experimental evidences that suggest nuclear shell model?

3

5. (a) Establish a relation between Einstein's Spontaneous and Stimulated coefficients.

(b) Calculate the Surface energy and Coulomb energy for a $_{92}^{236}$ U nucleus.

1+1

(c) Among 3Li⁷ and 4Be⁹ — Which nucleus is more stable?

2

(d) How does pair production take place by a high energy 2-rays? Can pair production occur in free space?

2+1



B.Sc. Honours 4th Semester Examination, 2023

PHSACOR10T-PHYSICS (CC10)

Time Allotted: 2 Hours

Full Marks: 40

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Candidates should answer in their own words and adhere to the word limit as practicable.

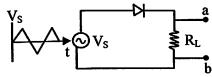
All symbols are of usual significance.

Question No. 1 is compulsory and answer any two from the rest

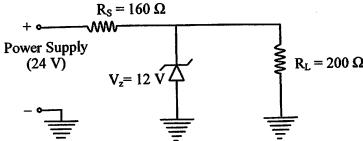
1. Answer any *ten* questions from the following:

 $2 \times 10 = 20$

- (a) For an unbiased p-n junction diode, sketch the variation of space charge, electric field and potential as a function of distance across the junction.
- (b) What is meant by diffusion capacitance of a p-n junction?
- (c) Can a voltmeter measure the built-in-barrier potential across the abrupt or step p-n junction?
- (d) What are the sources of instability of Q-point for CE amplifier?
- (e) Why do Si or Ge diodes not emit light but GaAs diodes do?
- (f) How can you use a bipolar junction transistor (BJT) as a switch?
- (g) Draw the waveform that will be shown in a CRO across a-b



(h) In the Zener regulator circuit shown below, calculate current through the series resistance (R_S)



- (i) Why the noise behaviours of JFET is less than that of a BJT?
- (j) How is a power amplifier different from a voltage amplifier?
- (k) Explain the current-voltage characteristics of a solar cell.
- (I) A Zener diode with break-down voltage 6 V is connected in series with a 100Ω resistance and a load of $0.5\,\mathrm{k}\Omega$ connected across the diode. The maximum allowable current through the Zener diode is $30\,\mathrm{mA}$. Calculate the operating range of the input voltage.

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- (m) If the input of an OPAMP integrator circuit is 1 volt then find and draw the nature of the output voltage. Assume $R = 1 \, M\Omega$ and $C = 2 \, \mu F$.
- (n) An amplifier has a voltage gain of -100 and a feedback ratio of -0.04. Find (i) the output voltage of the feedback amplifier for an input voltage of 60 mV and (ii) find the feedback voltage.
- (a) A full wave rectifier is operated from 50 Hz supply with 60 V (r.m.s.). It is connected to a load drawing a current of magnitude 200 mA and using 100 μF filter capacitor. Calculate the d.c. output voltage and the r.m.s. value of ripple voltage. Also calculate the ripple factor.
 - (b) Draw the circuit diagram of a logarithmic amplifier and a comparator using OPAMP and derive an expression for output voltage for the logarithmic amplifier.
- 3. (a) Draw a labeled circuit diagram of a two-stage R-C coupled amplifier. Find the mid-frequency gain of the amplifier with the help of an ac equivalent circuit. Explain why the gain of R-C coupled amplifiers falls at high frequencies.
 - (b) A two-stage RC coupled amplifier uses transistors having h-parameters $h_{\rm ie} = 1500 \,\Omega$ and $h_{\rm fe} = 250$. If the load resistance is $10 \, \rm k\Omega$, find the value of the coupling capacitor for having a lower cut-off frequency of 10 Hz.
- 4. (a) Define "Slew rate". Find the input signal maximum frequency for a specified 1+2 "Slew rate" of an OP-AMP.
 - (b) Is an external input signal necessary for the output of an oscillator? If not, how are oscillations initiated?
 - (c) Explain the working principle of Colpitts oscillator circuit using BJT.
- 5. (a) What are the fundamental differences between Class A and Class C amplifiers?
 - (b) Negative feedback reduces the gain of an amplifier still this feedback is widely used, why?
 - (c) What is JFET? An *n*-channel Si (having dielectric constant 12) JFET with a channel width of 0.06 cm is doped with a concentration $N_d = 10^{21} \,\mathrm{m}^{-3}$. Find the pinch off voltage.
 - (d) An *n* channel FET has $I_{DSS} = 8$ mA, $V_p = -4$ volt. Find V_{GS} that will result in a drain current of 4.5 mA.



B.Sc. Honours/Programme 4th Semester Examination, 2023

PHSHGEC04T/PHSGCOR04T-PHYSICS (GE4/DSC4)

Time Allotted: 2 Hours

Full Marks: 40

The figures in the margin indicate full marks. Candidates should answer in their own words and adhere to the word limit as practicable. প্রান্তিক সীমার মধ্যস্থ সংখ্যাটি পূর্ণমান নির্দেশ করে। পরীক্ষার্থীরা নিজের ভাষায় যথা সম্ভব শব্দসীমার মধ্যে উত্তর করিবে।

All symbols are of usual significance.

Question No. 1 is compulsory and answer any *two* from the rest ১ নং প্রশ্ন আবশ্যিক এবং অন্য প্রশ্ন থেকে যে-কোনো দুটি প্রশ্নের উত্তর দাও

Answer any ten questions from the following:
 নিম্নলিখিত যে-কোনো দশটি প্রশ্নের উত্তর দাওঃ

 $2 \times 10 = 20$

- (a) Find the dimension of viscosity coefficient. সাম্রতাঙ্কের মাত্রা বের করো।
- (b) What is Wavefront? তরক্ষমুখ বলতে কি বোঝো ?
- (c) State the differences between interference and diffraction. ব্যতিচার ও অপবর্তনের মধ্যে পার্থক্যগুলি লেখো।
- (d) What are beats? স্থরকম্প কাকে বলে ?
- (e) Define nodes and anti-nodes for a standing wave. স্থানুতরঙ্গের নিস্পন্দ ও সুস্পন্দ বিন্দুর সংজ্ঞা লেখো।
- (f) Write two applications of Polaroids. পোলারয়েড-এর দুটি ব্যবহার লেখো।
- (g) What is the intensity of a 60 dB Sound? একটি 60 dB শব্দের তীব্রতা কত ?
- (h) What will be the polarisation angle if the critical angle for a refracting Surface is 30°? কোনো প্রতিসারক তলের সংকট কোণ 30° হলে তার সমবর্তন কোণ কত হবে ?
- (i) Distinguish between Fresnel and Fraunhoffer class of diffraction. ফ্রেনেল ও ফ্রনহফার শ্রেণী অপবর্তনের মধ্যে পার্থক্য লেখো।
- (j) What is a zone plate? মণ্ডলফলক কী ?
- (k) What is angle of contact? স্পর্শকোণ বলতে কি বোঝো ?
- (l) What are the conditions for sustainable interference? স্থায়ী ব্যতিচারের শর্তগুলি কী কী ?

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- (m) Why are the Newton's rings circular? নিউটন রিংগুলি বৃত্তাকার হয় কেন ?
- (n) Light is an electromagnetic wave. Explain. আলো একটি তড়িংচুম্বকীয় তরঙ্গ ব্যাখ্যা করো।

$10 \times 2 = 20$ Answer any two questions from the following নিম্নলিখিত যে-কোনো দটি প্রশ্নের উত্তর দাও 2. (a) Establish Poiseuille's equation for flow of a liquid through horizontal capillary tube. 5 অনভমিক কৈশিক নলের মধ্যে দিয়ে তরলের প্রবাহ সম্পর্কিত Poiseuille's সমীকরণটি প্রতিষ্ঠা করো। (b) Show that in interference phenomenon energy is neither created nor destroyed but 3 is conserved. ব্যতিচার ঘটনায় শক্তির সৃষ্টি বা ধ্বংস কোনটাই হয় না কিন্তু শক্তির সংরক্ষণ হয় — প্রমাণ করো। 2 (c) Differentiate between bel and phon. বেল ও ফনের মধ্যে পার্থকা করো। 1+1 3. (a) What is diffraction? Define grating element. অপবর্তন বলতে কি বোঝো ? গ্রেটিং উপাদান বলতে কি বোঝায় ? 1+3 (b) What are beats? Show that the beat frequency is equal to the difference between the frequencies of the component oscillations. স্বরকম্প কাকে বলে ? দেখাও যে এর কম্পাঙ্ক হবে এর উপাদান দুটির কম্পাঙ্কের পার্থক্যের সমান। 2 (c) What do you mean by "Sharpness of Resonance"? ''অনুনাদের তীক্ষ্ণতা'' বলতে কি বোঝো ? 2 (d) State Brewster's Law in polarization of light. আলোর সমবর্তনে ব্রুস্টারের সূত্রটি বিবৃত করো। 4. (a) Derive an expression for the excess pressure inside a curved liquid film. 5 বক্রসরের অভান্তরস্থ অতিরিক্ত চাপের রাশিমালা নির্ণয় করো। 2+2 (b) What are the similarities and dissimilarities between zone plate and convex lens? বলয়পাত ও উত্তল লেন্সের মধ্যে সাদৃশ্য ও বৈসাদৃশ্য আলোচনা করো। 1 (c) What is double refraction? দ্বিপ্রতিসরণ বলতে কি বোঝো ? 5. (a) Write down the equation of a progressive wave. Explain mathematically the 1+4 formation of stationary waves by the superposition of two progressive waves. চলতরঙ্গের সমীকরণ লেখো। দুটি চলতরঙ্গের উপরিপাতের ফলে কীভাবে স্থানুতরঙ্গের সৃষ্টি হয় তা গাণিতিক বিশ্লেষণ দ্বারা দেখাও। (b) Why do two stream line can not intersect each other? 2 দুটি ধারা রেখ কেন একে অপরকে ছেদ করে না ? (c) In a Newton's ring experiment, the diameter of 15th ring was found to be 0.590 cm 3 and that of the 5th ring was 0.336 cm. If the radius of curvature of the Planoconvex lens is 100 cm, calculate the wavelength of light used. নিউটন-এর রিং পরীক্ষায় 15th রিং-এর ব্যাস 0.590 cm এবং 5th রিং-এর ব্যাস 0.336 cm। সমতলোত্তল লেন্দের বক্রতা ব্যাসার্ধ 100 cm হলে, ব্যবহৃত আলোর তরঙ্গদৈর্ঘ্য কত ?